## CHAPTER 1: FUNCTIONS

## (4) Cloned SPM Question (2006, Paper 1)

In the diagram, set $Y$ shows the images of certain elements of set $X$.

(a) State the type of relation between set $X$ and set $Y$.
(b) Using the function notation, write a relation between set $X$ and set $Y$.

## Solution

(a) Many-to-one relation
(b) $\quad f: x \rightarrow x^{2}$ or $f(x)=x^{2}$

## Pointers

- Both -3 and 3 are mapped onto one image only, that is, 9 , both -4 and 4 are mapped onto one image, that is, 16 , therefore the type of relation is many-to-one.
- Since $f(-3)=(-3)^{2}=9, f(3)=3^{2}=9, f(-4)=(-4)^{2}=16$ and $f(4)=4^{2}=16$, the notation is $f: x \rightarrow x^{2}$ or $f(x)=x^{2}$.


## Cloned SPM Question (2006, Paper 1)

The diagram shows the function $p: x \rightarrow \frac{x-k}{x}, x \neq 0$, where $k$ is a constant.


Find the value of $k$.

## Solution

$p(x)=\frac{x-k}{x}, x \neq 0$
From the diagram, $p(10)=\frac{3}{5}$.
Thus, $\frac{10-k}{10}=\frac{3}{5}$
$10-k=6$
$k=4$

## Pointers

- From the arrow diagram, we can write $p(10)=\frac{3}{5}$.
- Substitute $x=10$ into the equation $\frac{x-k}{x}=\frac{3}{5}$ to find the value of $k$.

